

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

GCSE MATHEMATICS

H

Higher Tier

Paper 3 Calculator

Monday 13 November 2023

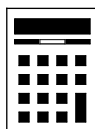
Morning

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
26	
TOTAL	

Advice

In all calculations, show clearly how you work out your answer.



3 The length of a line is 8 cm to the nearest centimetre.

Complete the error interval.

[2 marks]

Answer _____ cm \leq length < _____ cm

4 At what point does the graph $y = x^3 - 1$ cross the y axis?

[1 mark]

Answer (_____ , _____)

Turn over for the next question



8 Circle the largest number.

[1 mark]

5.30 $\dot{4}$

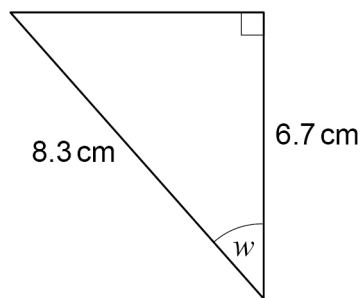
5.344

5.34

5.3 $\dot{4}$

9 Use trigonometry to work out the size of angle w .

[3 marks]

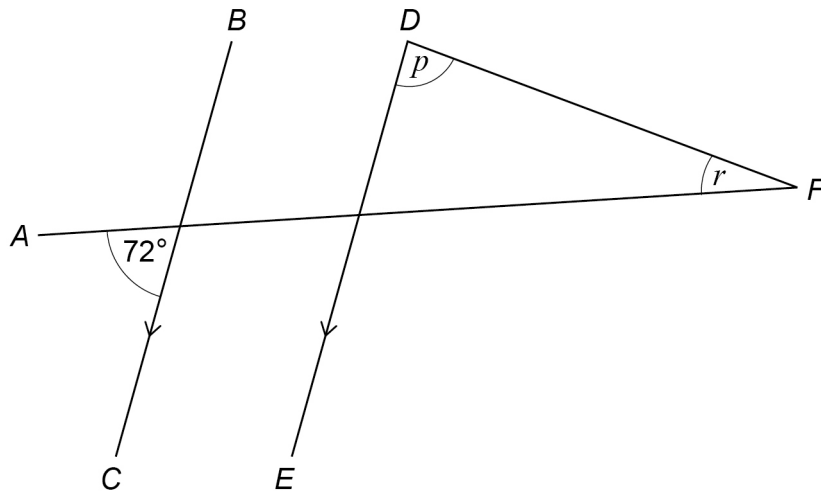


Not drawn
accurately

$w =$ _____ $^{\circ}$



12

 AF , BC , DE and DF are straight lines. BC and DE are parallel.Not drawn
accurately p is three times r .Work out the size of angle p .**[3 marks]**

$$p = \underline{\hspace{2cm}}^{\circ}$$



- 13** 100 people were asked about the distance they travel from home to work.
The table shows information about the results.

Distance, d (miles)	Frequency
$0 \leq d < 5$	21
$5 \leq d < 10$	24
$10 \leq d < 20$	37
$20 \leq d < 40$	18

- 13 (a)** Write down the **greatest** possible number of people who work from home.

[1 mark]

Answer _____

- 13 (b)** One person is chosen at random.

Work out the probability that the person travels **at least** 10 miles.

[1 mark]

Answer _____

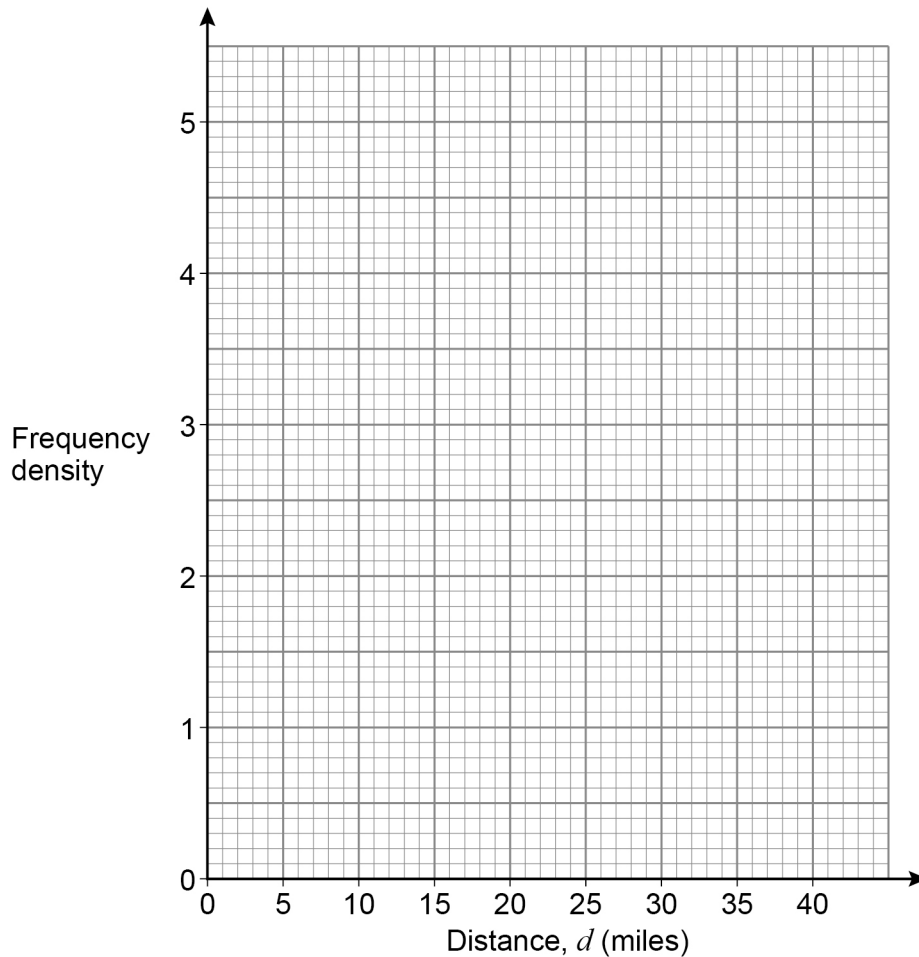


13 (c) The table is repeated.

Distance, d (miles)	Frequency
$0 \leq d < 5$	21
$5 \leq d < 10$	24
$10 \leq d < 20$	37
$20 \leq d < 40$	18

Draw a histogram to represent the results.

[3 marks]



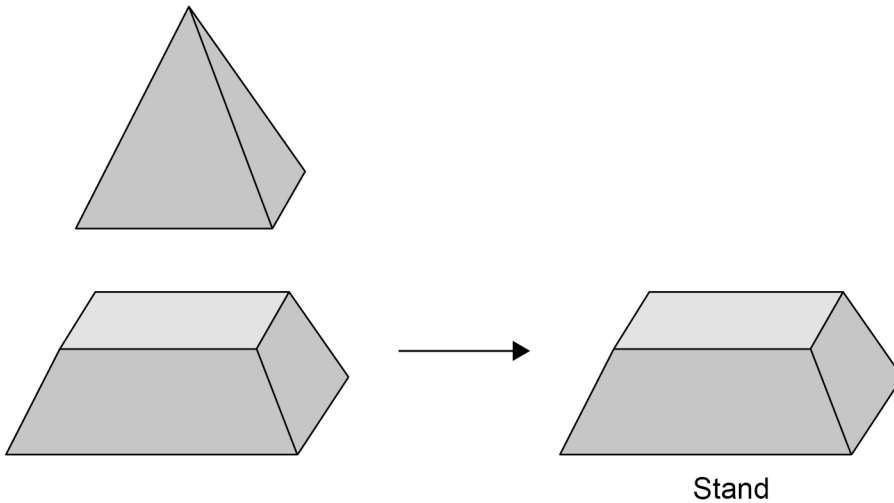
- 14 A solid trophy consists of a stand and a player.



Trophy

The stand is made by removing a small pyramid from a large pyramid.

Large pyramid	Square base, edge 8 cm	Perpendicular height 16 cm
Small pyramid	Square base, edge 5 cm	Perpendicular height 10 cm



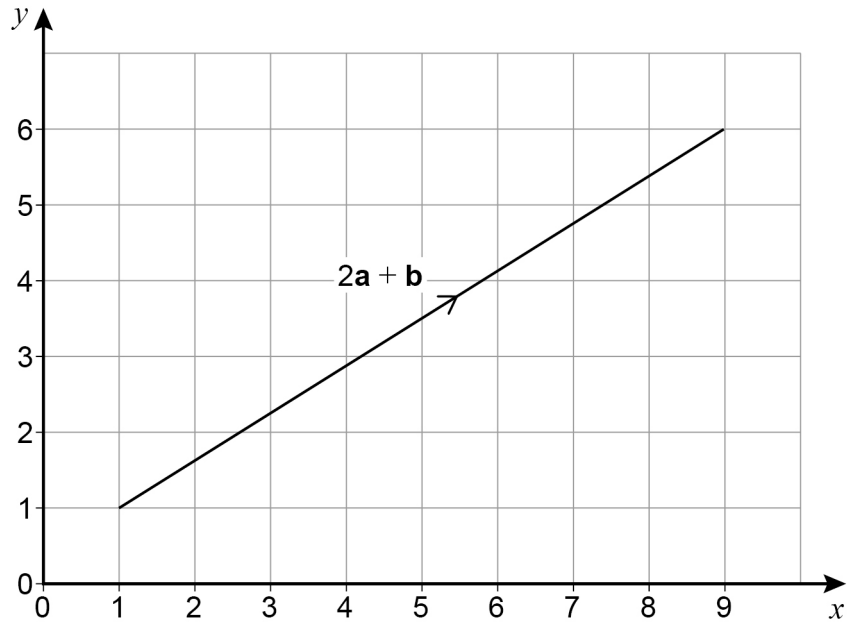
Stand

$$\text{Volume of a pyramid} = \frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$$



15 $\mathbf{a} = \begin{pmatrix} m \\ 3 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} -4 \\ p \end{pmatrix}$

The diagram shows the vector $2\mathbf{a} + \mathbf{b}$



Work out the values of m and p .

[4 marks]

$m =$ _____ $p =$ _____

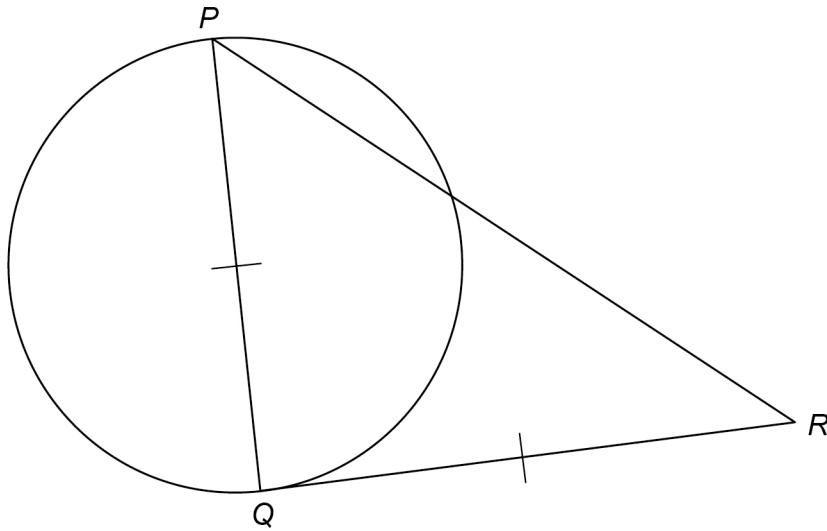


16

 PQ is a diameter of a circle. QR is a tangent to the circle.

$$PQ = QR$$

$$PR = 10 \text{ cm}$$

Not drawn
accuratelyWork out the **radius** of the circle.

Give your answer as a decimal.

[3 marks]

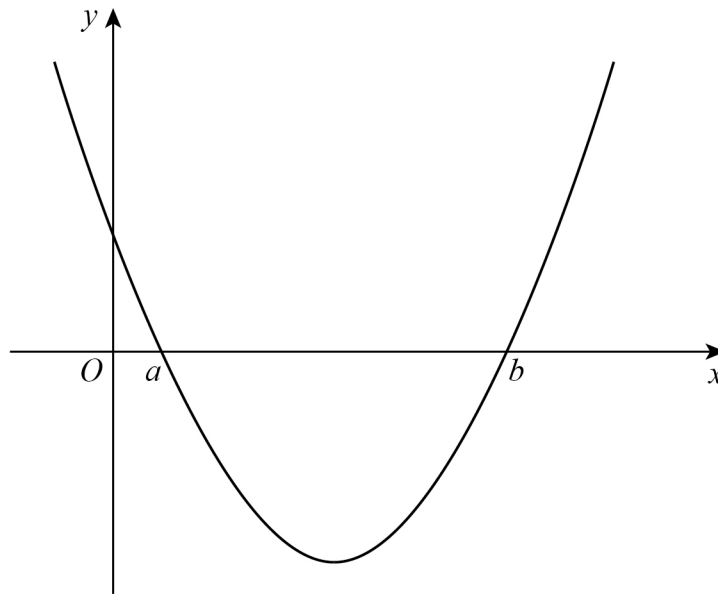
Answer _____ cm



17

Here is a sketch of the quadratic graph $y = f(x)$

The graph crosses the x -axis at $x = a$ and $x = b$



Write an expression for the x -coordinate of the turning point.

[1 mark]

Answer _____



18 Simplify $\frac{2(x+4)^5}{(x+4)^3}$

Give your answer in the form $ax^2 + bx + c$ where a , b and c are integers.

[3 marks]

Answer _____

Turn over for the next question



20 Solve $2x(x + 10) = 5x - 18$

[4 marks]

Answer _____

Turn over for the next question

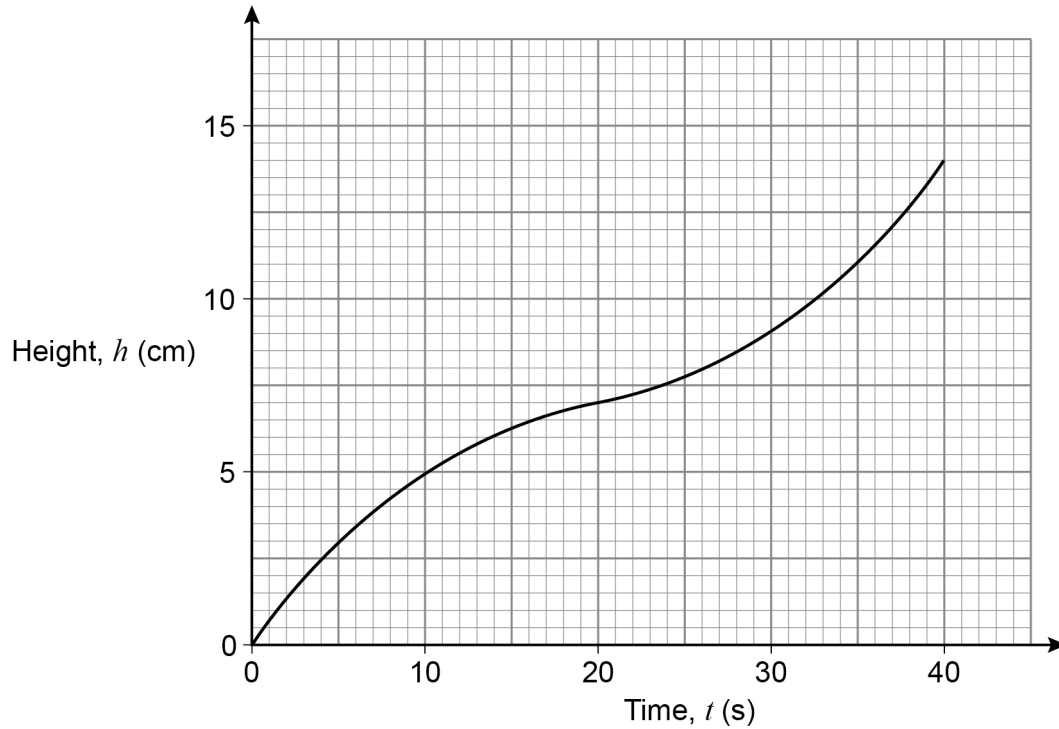


21

Water flows from a tap at a constant rate.

A container is filled with water from the tap in 40 seconds.

The graph shows the height, h centimetres, of the water after time, t seconds.

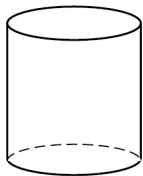


21 (a) The container is one of these shapes.

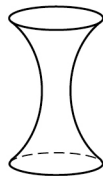
Circle the letter of the correct shape.

[1 mark]

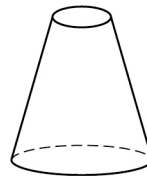
A



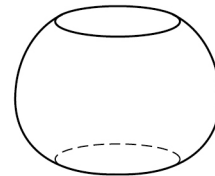
B



C



D



- 21 (b) By drawing a tangent on the graph,
estimate the rate at which the height is increasing when $t = 10$

[2 marks]

Answer _____ cm/s

- 22 Write $\frac{7}{2a^2} - \frac{3}{5a}$ as a single fraction in its simplest form.

[2 marks]

Answer _____



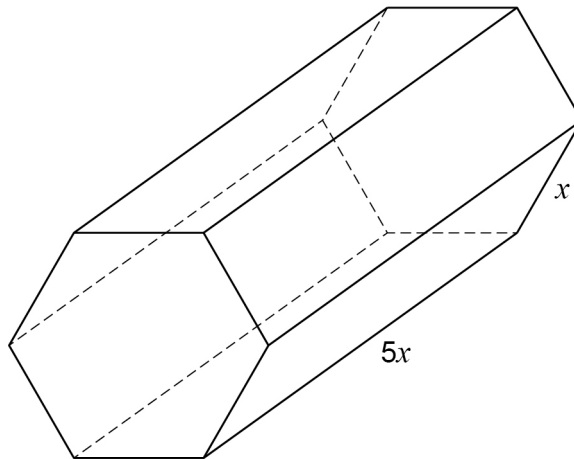
23

A chocolate box in the shape of a prism is being designed.

All lengths are in centimetres.

The cross section is a regular hexagon with side x

The length is $5x$



An expression for the area of the cross section, in cm^2 , is $\frac{3\sqrt{3}}{2}x^2$

The **total** surface area of the box must be less than 650 cm^2

Work out the largest possible **integer** value of x .

You **must** show your working.

[4 marks]

Answer _____



25

 a is three quarters of c

$$6b = 5c$$

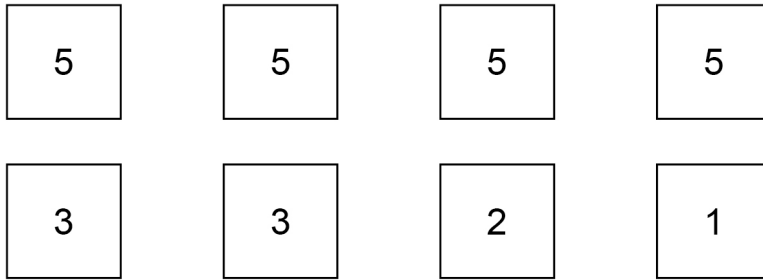
Work out the ratio $a : b : c$ Give your answer in its simplest form, where a , b and c are integers.**[3 marks]**

Answer _____ : _____ : _____



26

In a game, these numbered tiles are in a bag.



To play the game

Choose tiles at random one at a time and do not replace the tiles.
You win if at any stage the total of the numbers on your tiles is 10

Amber plays the game once.

Work out the probability that she wins.

[4 marks]

Answer _____

7

Turn over ►



27 (a) The graph of $y = x^3$ is translated to the graph of $y = (x - 2)^3$

Write down the translation vector.

[1 mark]

Answer $\left(\quad \right)$

27 (b) The graph of $y = 5x + 4$ is reflected in the y -axis.

Write down the equation of the reflected graph.

[1 mark]

Answer _____

END OF QUESTIONS

